### YEAR 9 - DEVELOPING NUMBER

# Standard Form

### What do I need to be able to do?

By the end of this unit you should be able to:

- Write numbers in standard form and as ordinaru numbers
- Order numbers in standard form
- Odd/ Subtract with standard from
- Multiply/ Divide with standard form
- Use a calculator with standard form

#### Keywords

Standard (index) Form: O sustem of writing very big or very small numbers

Commutative: an operation is commutative if changing the order does not change the result

Base: The number that gets multiplied by a power

**Power:** The exponent — or the number that tells you how many times to use the number in multiplication.

**Exponent**: The power — or the number that tells you how many times to use the number in multiplication **Indices**: The power or the exponent.

Negative: a value below zero.

#### Positive powers of 10

l billion - 1 000 000 000

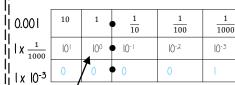
Oddition rule for indices  $10^a \times 10^b = 10^{a+b}$ 

Subtraction rule for indices  $10^a \div 10^b = 10^{a-b}$ 

#### Standard form with numbers > 1

Onu number between I and less than 10 - A x 10 n 4

Negative powers of 10



Example

3.2 x 10 4

ll = 32000

= 3.2 x 10 x 10 x 10 x 10

0.8 × 10 4 53x 10(07)

Non-example

Ony value to the power O always = 1

Negative powers do not indicate negative solutions

#### Numbers between 0 and 1

0.054  $= 5.4 \times 10^{-2}$ 

1	$\frac{1}{10}$	$\frac{1}{100}$	$\frac{1}{1000}$
100	10-1	10-2	10-3
0	• 0	5	4

O negative power does not mean a negative answer — it means a number closer to 0

#### Order numbers in standard form

 $6.4 \times 10^{-2}$  $2.4 \times 10^{2}$ 

 $1.3 \times 10^{-1}$ 3.3 x 100

Look at the power first

0.064

240

0.13

will the number be = > or < than I Use a place value arid to compare the

numbers for orderina

This is not the -

final answer

#### Mental calculations

6.4 x 10<sup>2</sup> x 1000 Not in Standard Form

 $6.4 \times 10^{2} \times 10^{3}$ 

= 6.4 x 10<sup>5</sup>

Use addition for indices rule

Divide the values

=  $24 \times 10^5$  Not in Standard Form 1

=  $2.4 \times 10^{1} \times 10^{5}$  Use addition for

 $8x 10^5 x3$ 

 $= 2.4 \times 10^{6}$ 

indices rule.

#### $(2 \times 10^3) \div 4$

 $= (2 \div 4) \times 10^3$ 

 $= 0.5 \times 10^3$ 

#### Remember the layout for standard form

. Ony integer Ony number A x 10 n 4 between I and

#### Oddition and Subtraction

Tip: Convert into ordinary numbers first and back to standard from at the end

Method I

= 600000 + 800000

= 1400000

= 1.4 x 10<sup>5</sup>

More robust method

Less room for misconceptions Easier to do calculations with negative indices Can use for different powers

6 x 105 + 8 x 105 Method 2

> $= (6 + 8) \times 10^{5}$ = 14 x 10<sup>5</sup>

1.4 x 101 x 105

= 1.4 x 10<sup>5</sup>

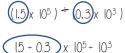
Only works if the powers are the same

### Multiplication and division

Division auestions can look like this

less than 10

For multiplication and division you can look at the values for A and the powers of 10 as two separate calculations



Revisit addition and subtraction laws for indices they are needed for the calculations

 $=5 \times 10^{2}$ 

**Oddition** law for indices a m x a n = a m + n

Subtraction law for indices  $a^m \div a^n = a^{m-n}$ 

#### Using a calculator

 $14 \times 10^5 \times 39 \times 10^3$ 

Use a calculator to work out this question to a suitable degree of accuracy

Input 14 and press  $\boxed{\times 10^x}$  Then press 5 (for the power)

Input 3.9 and press **x10**° Then press 3 (for the power) Press 🔳

This gives you the solution

Click calculator for video tutorial

#### To put into standard form and a suitable degree of accuracy

Press SHIFT (SETUP) and then press 7 for sci mode. Choose a degree of accuracy so in most cases press 2

Onswer: 5.5 x 108

### YEAR 9 - REASONING WITH NUMBER

### Numbers

### What do I need to be able to do?

By the end of this unit you should be able to:

- Identify integers, real and rational numbers
- Solve problems with number
- Work with directed number
- Find HCF/ LCM
- Odd/ Subtract fractions
- Multiply/ Divide fractions
- Write numbers in standard form

### Keywords

Integer: a whole number that is positive or negative

Rational: a number that can be made by dividing two integers

Irrational: a number that cannot be made by dividing two integers

**Inverse operation**: the operation that reverses the action

Quotient: the result of a division **Product**: the result of a multiplication.

Multiples: found by multiplying any number by positive integers

Factor: integers that multiply together to get another number

#### Integers, real and rational numbers

Rational — root word: ratio

**Real numbers**:  $\frac{2}{3}$  stems from 2:1 ( $\frac{2}{3}$  of the whole)

Irrational numbers:  $\sqrt{2}$  the solution is a decimal that never ends and does not repeat.

The square root of a negative is not a real number and cannot be found



Common factors are factors two or more numbers share

HCF — Highest common factor

HCF of 18 and 30



#### LCM — Lowest common multiple

LCM of 9 and 12

9, 18, 27, 36, 45, 54

12, 24, 36, 48, 60

LCM = 36

The first time their multiples match

#### Standard form any number A x 10 n

between I and less than 10

6 x 105 + 8 x 105  $(1.5 \times 10^5) \div (0.3 \times 10^3)$ 

- = 600000 + 800000
- = 1400000

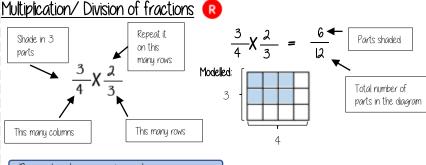
= 1.4 x 10<sup>5</sup>

 $=5 \times 10^{2}$ 

 $15 \div 0.3 \times 10^5 \div 10^3$ 

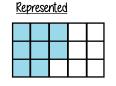
Oddition/Subtraction of fractions 👩 ========

#### Directed number $\bigcirc$ = 1 **Oddition** Multiplication Generalisation + - = -The act of counters 7ero pair into their (- | + | = () ) negative is turning -2x-3=6Subtraction them over Generalisation Divisions are the inverse operations "Subtract" — means take b = -4a = 5Representation for calculation away or <u>remove</u> Brackets around negative substitutions helps remove calculation errors Take away one $2a - b = 2 \times 5 - (-4) = 10 + 4 = 14$



#### Remember to use reciprocals

Multiplying by a reciprocal gives the same outcome.



Use equivalent fractions

to find a common

multiple for both denominators

# YEAR 9 - REASONING WITH NUMBER...

# Using Percentages

# What do I need to be able to do?

#### By the end of this unit you should be able to:

- Use FDP equivalence
- Calculate percentage increase and decrease
- Express percentage change
- Solve reverse percentage problems
- Solve percentage problems (calculator and non calculator problems)

#### Keywords

Percent: parts per 100 — written using the / symbol

**Decimal**: a number in our base 10 number system. Numbers to the right of the decimal place are called decimals. **Fraction**: a fraction represents how many parts of a whole value you have.

i | **Equivalent**: of equal value.

Reduce: to make smaller in value.

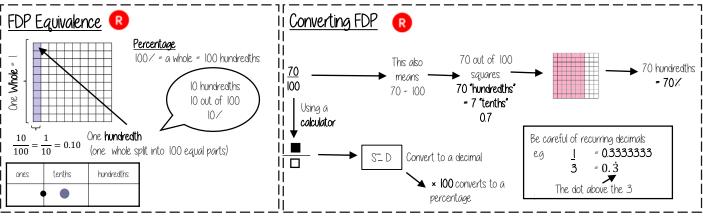
Growth: to increase / to grow.

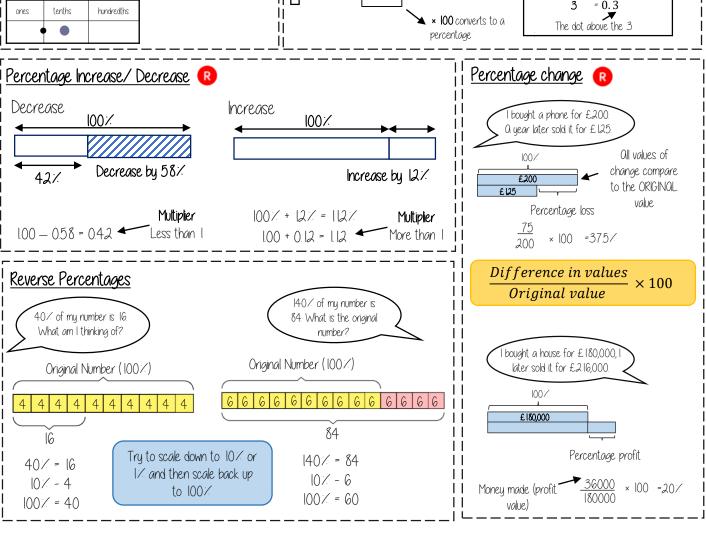
Integer: whole number, can be positive, negative or zero.

Invest: use money with the goal of it increasing in value over time (usually in a bank).

Multiplier: the number you are multiplying by.

| Profit: the income take away any expenses/ costs.





# YEAR 9 - REASONING WITH NUMBER

# Maths & Money

### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Solve problems with bills and bank statements
- Calculate simple interest
- Calculate compound interest
- Calculate wages and taxes
- Solve problems with exchange rates
- Solve unit pricing problems

#### Keywords

Credit: money being placed into a bank account

Debit: money that leaves a bank account

Balance: the amount of money in a bank account Expense: a cost/outgoing.

Deposit: an initial payment (often a way of securing an item you will later pay for)

Multiplier: a number you are multiplying by (Multiplier more than I = increasing, less than I = decreasing)

Per Onnum: each year

Currency: the type of money a country uses.

Unitary: one — the cost of one.

#### Bills and Bank Statements

Bills — tell you the amount items much money you need to pay!

Some can include a total
Look for different units
(Is it in pence or pounds)

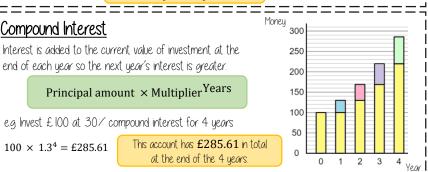
cost and can snow now				
Menu	Price			
Milk	89p			
Tea	£1.50			

#### Bank Statements

Bank statement can have negative balances if the money spent is higher than the money coming into the account

Date	Description	Credit	Debit	Balance
l <sup>qth</sup> Sept	Salary	£1500		£1500
19th Sept	Mortgage		£600	£900
25 <sup>th</sup> Setp	Bday Money	£15		£915

#### Money 300 Simple Interest For each year of investment the interest remains the same ~ Principal amount ×Interest Rate × Years Principal amount is the amount invested in the account. e.g Invest £100 at 30% simple interest for 4 years This account earned £120 interest. Ot the end of year 4 they have £220



#### Value Odded Tax (VOT)

VOT is payable to the government by a business. In the UK VOT is 20% and added to items that are bought.

Essential items such as food do not include VOT.

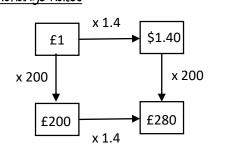
#### Waaes and Taxes

Salaries fall into tax brackets — which means theu pay this much each month from their salary.

Taxable Income	Tax Rate
£12 501 to £50 000	20%
£50 001 to £150 000	40%
over £150 000	45%



#### Exchange Rates



When making estimates it is also useful to use estimates to check if our solution is reasonable.

Use inverse operations to reverse the exchange process

Common Currencies		
United Kingdom	£	Pounds
United States of Omeric	ca \$	Dollars
Europe	€	Euros

#### Unit Pricina

4 Oranges £1

5 cupcakes £1.20

4 = £1.005 = £1.20÷ 5 2 = £0.50

1 = £0.251 = £0.20 To calculate unit per cost you divide by the cost.

Cupcakes are the best value as one item has the cheapest value

There is a directly proportional relationship between the cost and

### YEAR 9 - DEVELOPING NUMBER

### Number Sense

#### What do I need to be able to do?

By the end of this unit you should be able to:

- Round numbers to powers of 10 and 1 sf
- Round numbers to any dp
- Estimate solutions
- Calculate using order of operations
- Calculate with money, units of measurement and time

#### Keywords

Significant: Place value of importance

Round: Making a number simpler but keeping its value close to what it was.

**Decimal:** Place holders after the decimal point.

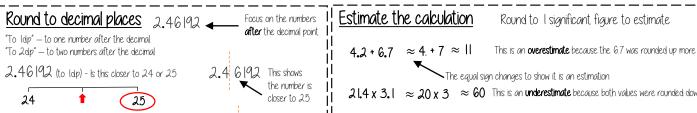
Overestimate: Rounding up — gives a solution higher than the actual value **Underestimate**: Rounding down — gives a solution lower than the actual value.

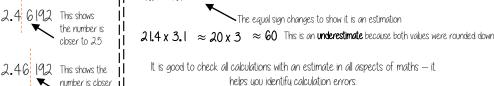
Metric: a system of measurement.

Balance: The amount of money in a bank account

Deposit: Putting money into a bank account

#### Round to powers of 10 and 1 sia figure 370 to I sianificant fiaure is 400 37 to I significant figure is 40 3.7 to I significant figure is 4 5475 to the nearest 10 5495 to the nearest 1000 5475 to the nearest 100 0.37 to 1 significant figure is 0.4 5480 5000 5400 6000 0.00037 to 1 significant figure is 0.0004 Round to the first non-zero number







Brackets Operations in brackets are calculated first

Calculations with money

Debit - You have £0 or more in an account

Money calculations are to 2dp



Multiplication/Division They are carried out in the order from left to right in the

2.46 192 (to 12dp) - Is this closer to 246 or 247

247

question Oddition/Subtraction

Other operations e.g. powers, roots,

Theu are carried out in the order from left to right in the

Credit - You have less than £0 in an account



Using a calculator — ensure you are working in the correct units.

£130 + 50p = 130 + 50 (in pence) 130 + 0.50 (in pouinds)

£1 = 100p



Units are important: Useful Conversions



### Metric measures of length

Kilo = 1000 x meter

Milli -  $\frac{1}{1000}$  x meter

### Units of weight/capacity

Weight = g, kg, t Capacity (volume of liquid) = ml, L

#### Time and the calendar



Leap Year - 366 days (every 4 years)



12 Months = one year = 52 weeks 31 days - Jan, March, May, July Oug, Oct, Dec 30 days - Opril, June, Sept, Nov

28 days — **Feb** (29 leap year)

<u>l week</u> — 7 days

I hour - 60 minutes I minute - 60 seconds

Iday - 24 hours

Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday Use a number line for time calculations!



Use am (morning) and pm (afternoon) Only use hour times up to 12



Digital Clock (24-hour times)

24-hour clock 0-11 (morning hours)

12-23 (afternoon hours)

## YEAR 9 - REASONING WITH GEOMETRY

# Solving ratio & proportion problems

### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Solve problems with direct proportion
- Use conversion graphs
- Solve problems with inverse proportion
- Solve ratio problems
- Solve 'best buy' problems

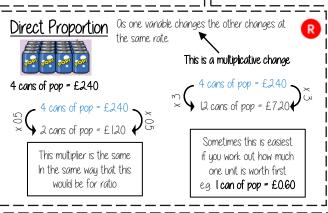
### !! Keywords

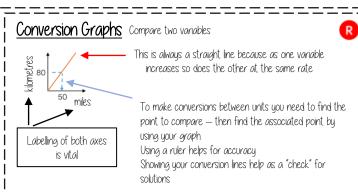
**Proportion**: a comparison between two numbers

Ratio: a ratio shows the relative size of two variables

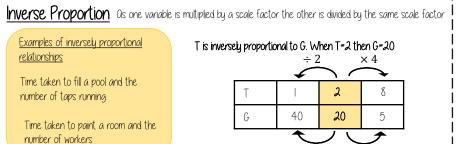
Direct proportion: as one variable is multiplied by a scale factor the other variable is multiplied by the same scale factor.

**Inverse proportion**:: as one variable is multiplied by a scale factor the other is divided by the same scale factor.





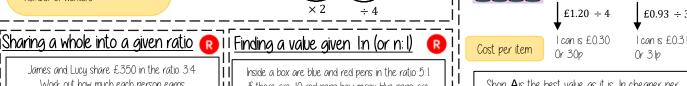
Best Buys



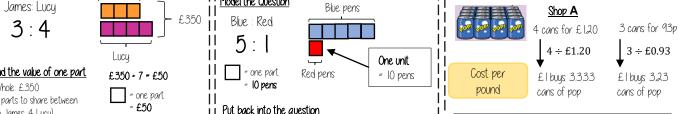


Have a directly proportional relationship



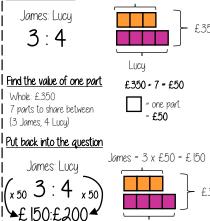


Work out how much each person earns Shop Ais the best value as it is lp cheaper per If there are 10 red pens how many blue pens are there? can of pop Model the Question lames Model the Question



Shop  ${\sf A}$  is still shown as being the best value but pay attention to the unit you are calculating, per item or per pound.

> Best value is the most product for the lowest price per unit



Lucy =  $4 \times £50 = £200$ 

<u>Put back into the question</u> Blue pens =  $5 \times 10 = 50$  pens Red pens =  $1 \times 10 = 10$  pens

There are 50 Blue Pens

# YEAR 9 - REASONING WITH GEOMETRY.

# Rates

# What do I need to be able to do?

#### By the end of this unit you should be able to:

- Solve speed, distance, time questions
- Use distance time graphs
- Solve density, mass, volume problems
- Solve flow problems
- Use flow graphs
- Interpret rates of change and their units

### <u>Keywords</u>

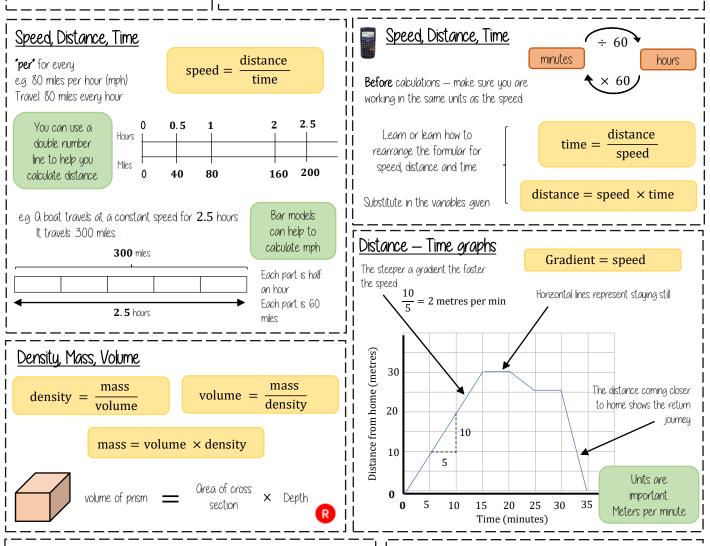
Convert: change

Mass: a measure of how much matter is in an object. Commonly measured by weight.

Origin: the coordinate (0, 0)

**Volume**: the amount of 3D space a shape takes up

Substitute: putting numbers where letters are — replacing numbers into a formula



### Flow problems & graphs

This will fill at a constant rate, then as the space decreases it will speed up and the neck of the bottle fill at a faster constant speed

The cylinder will fill at a constant speed

Units are important Ensure any volume calculations are the same unit as the rate of flow

# Revisit your conversions between units of length and capacity Speed: miles per hour Exchange rates: euros per pounds Density: mass per volume kilometres kilometres

### YEAR 9 - REASONING WITH ALGEBRA

# Forming and Solving Equations

### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Solve inequalities with negative numbers
- Solve equations with unknowns on both sides |
- Solve inequalities with unknowns on both
- Substitute into formulae and equations

### Keuwords

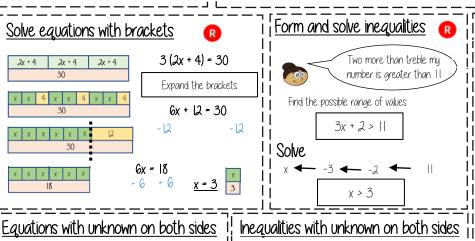
Inequality: an inequality compares who values showing if one is greater than, less than or equal to another

Variable: a quantity that may change within the context of the problem Rearrange: Change the order

**Inverse operation** the operation that reverses the action

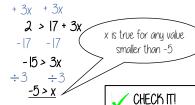
Substitute: replace a variable with a numerical value

Solve: find a numerical value that satisfies an equation Rearrange formulae

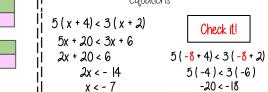




2 - 3x > 17

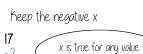


Solving inequalities has the same method as equations





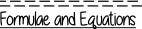
Method 2



2 - 3(-6) = 20TRUE/ CORRECT

true...

bigger than -5 -3x > 15÷-3 This cannot be x > -5



4x + 5 = 3x + 24

x + 5 = 24

x = 19

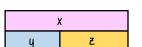
-3x

Formulae — all expressed in symbols

Equations — include numbers and can be solved |

When you multiply or divide x by a negative you need to reverse the

#### Rearranging Formulae (one step)

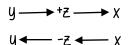


X = y + Z

Substitute in values

Rearrange to make y the subject.

y = x - Z



Using inverse operations or fact families will guide you through rearranging formulae

Rearrange

Rearranging can also be checked by substitution.

Language of rearranging...

Make XXX the subject

Change the subject

### Rearranging Formulae (two step)

In an equation (find x) 4x - 3 = 9

-20 IS smaller than -18

In a formula (make x the subject) xy - s = a

+3 4x = 12

+ 5 + 5 xu = a + s÷ y ÷ y

 $X = \alpha + S$ 

The steps are the same for solving and rearranging

Rearranging is often needed when using y = mx + c

e.g. Find the gradient of the line 2y - 4x = 9

Make y the subject first y = 4x + 9

Gradient = 4= 2

# YEAR 9 - REASONING WITH ALGEBRA

# Straight Line Graphs

#### What do I need to be able to do?

By the end of this unit you should be able to:

- Compare gradients
- Compare intercepts
- Understand and use y= mx + c
- Find the equation of a line from a graph
- Interpret gradient and intercepts of reallife graphs

#### Keywords

Gradient: the steepness of a line

Intercept: where two lines cross. The y-intercept: where the line meets the y-axis.

Parallel two lines that never meet with the same gradient.

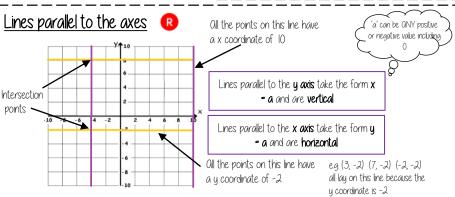
Co-ordinate: a set of values that show an exact position on a graph.

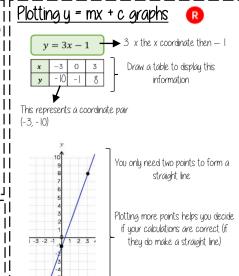
Linear: linear graphs (straight line) — linear common difference by addition/subtraction

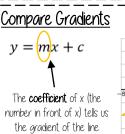
Osymptote: a straight line that a graph will never meet.

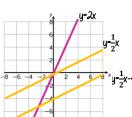
Reciprocal: a pair of numbers that multiply together to give 1.

I I Perpendicular: two lines that meet at a right angle





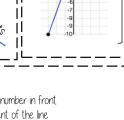




The **areater** the gradient — the steeper the line

> Parallel lines have the same gradient

Softing design

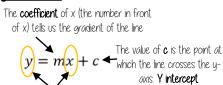


Remember to join the points to make

The equation of a line can be rearranged: E.g.:

u = c + mx

#### Compare Intercepts y = mx + (c) which the line crosses the y-The value of c is the point at axis. Y intercept The coordinate of a y intercept will always be (0,c) Lines with the same uintercept cross in the same



which the line crosses the y-

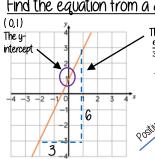
c = y - mxIdentify which coefficient you are identifying or

The u-intercept shows the

minimum charge.

The gradient represents the price per mile

#### Find the equation from a graph



The Gradient  $\frac{6}{2} = 2$ 

v = 2x + 1

The direction of the line indicates a positive

Negative gradients

#### Real life graphs

y and x are coordinates

y = mx + c

A plumber charges a £25 callout fee, and then £12.50 for every hour. Complete the table of values to show the cost of hiring the plumber.

In real life graphs like this values will always be positive because they

measure distances or objects which cannot be negative

<u>Direct Proportion graphs</u> To represent direct proportion the graph must start at the origin.

When you have 0 pens this has 0 cost. The gradient shows the

	ns costs £2 he table of v		ow the cost	of buying t	ooxes of pe
Boxes	0	1	2	3	8
Cost (E)		6230			

# YEAR 9 - REPRESENTATIONS

Algebraic Representation

### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Draw quadratic graphs
- Interpret quadratic graphs
- Interpret other graphs including reciprocals
- Represent inequalities

### Keywords

Quadratic: a curved graph with the highest power being 2. Square power.

Inequality: makes a non equal comparison between two numbers

**Reciprocal**: a reciprocal is 1 divided by the number

**Cubic**: a curved graph with the highest power being 3. Cubic power.

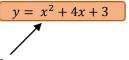
Origin: the coordinate (0, 0)

Parabola: a 'u' shaped curve that has mirror symmetry

Intersection with

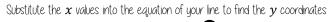
the  $\gamma$  axis

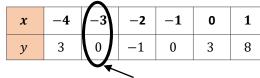
#### Quadratic Graphs



If  $x^2$  is the highest power in your equation then you have a quadratic graph.

It will have a parabola shape





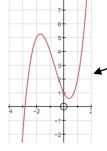
Coordinate pairs for plotting (-3,0)

Plot all of the coordinate pairs and join the points with a curve (freehand) Quadratic graphs are always symmetrical with the turning point in the middle

#### Interpret other graphs

Cubic Graphs

$$y = x^3 + 2x^2 - 2x + 1$$



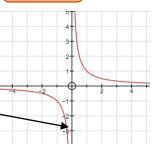
If  $x^3$  is the highest power in your equation then you have a <u>cubic graph</u>

> Reciprocal graphs never touch the  $\nu$  axis.

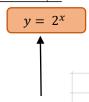
This is because x cannot be 0This is an asymptote



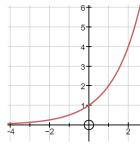




Exponential Graphs



Exponential graphs have a power of x

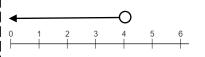


#### Represent Inequalities

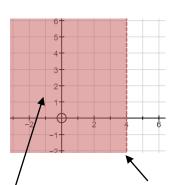
Multiple methods of representing inequalities



Oll values are less than 4

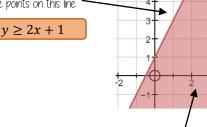


The shaded area indicates all possible values of x



the points on this line

The solid line shows that the inequality includes all



The shaded area indicates all possible solutions to this inequality

The dotted line shows that the inequality does not include these points

## YEAR 9 - DEVELOPING GEOMETRY...

# Line symmetry and reflection

### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Recognise line symmetry
- Reflect in a horizontal line
- Reflect in a vertical line
- Reflect in a diagonal line

#### Keywords

**Mirror line**: a line that passes through the center of a shape with a mirror image on either side of the line **Line of symmetry**: same definition as the mirror line

Reflect: mapping of one object from one position to another of equal distance from a given line.

Vertex: a point where two or more-line segments meet.

Perpendicular: lines that cross at 90°

Horizontal: a straight line from left to right (parallel to the x axis)

Vertical: a straight line from top to bottom (parallel to the y axis)

#### <u>Lines of symmetry</u>

Mirror line (line of reflection)



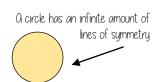
Parallelogram

No lines of symmetry  $\angle$ 

Rhombus

two lines of summetry

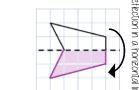
Shapes can have more than one line of symmetry... This regular polygon (a regular pentagon has 5 lines of symmetry)







Note: a reflection doubles the area of the original shape

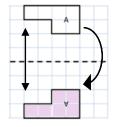


Reflection in the line x=2

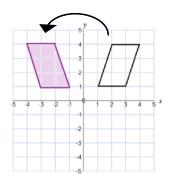
Reflection on an axis grid

#### Reflect horizontally/vertically(2)

All points need to be the same distance away from the line of reflection



Reflection in the line y axis — this is also a reflection in the line x=0



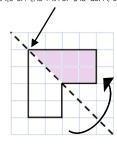
#### Lines parallel to the x and y axis

REMEMBER

Lines parallel to the x-axis are y = \_\_\_\_ Lines parallel to the y-axis are x = \_\_\_\_

#### <u>| Reflect Diagonally(1)</u>

Points on the mirror line don't change position

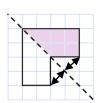


Fold along the line of symmetry to check the direction of the reflection

#### Turn your image

If you turn your image it becomes a vertical/ horizontal reflection (also good to check your answer this way)



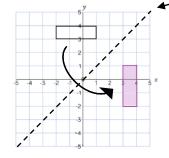


#### Drawing perpendicular lines

Perpendicular lines to and from the mirror line can help you to plot diagonal reflections

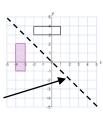
#### Reflect Diagonally (2)

This is the line **y = x** (every y coordinate is the same as the x coordinate along this line)



П

This is the line **y = - x**The x and y coordinate have the same value but opposite sign



#### <u>Turn your image</u>

If you turn your image it becomes a vertical/ horizontal reflection (also good to check your answer this way)

# YEAR 9 - REASONING WITH GEOMETRY... Rotation & Translation

#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Identify the order of rotational symmetry
- Rotate a shape about a point on the
- Rotate a shape about a point not on a
- Translate by a given vector
- Compare rotations and reflections

#### Keywords

Rotate: a rotation is a circular movement

Symmetry: when two or more parts are identical after a transformation.

Reaular: a regular shape has angles and sides of equal lengths. **Invariant**: a point that does not move after a transformation.

Vertex: a point two edges meet. Horizontal: from side to side

Vertical: from up to down

### <u>Rotational Symmetry</u>



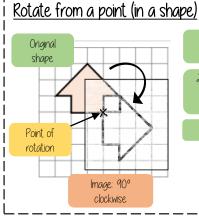
Tracing paper helps check rotational summetru

I. Trace your shape (mark the centre point)



3. Count the times it fits back into itself

O regular pentagon has rotational symmetry of order 5



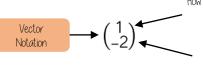
I. Trace the original shape (mark the point of rotation)

2 Keep the point in the same place and turn the tracing

3. Draw the new shape

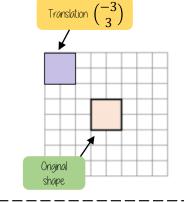


### Translation and vector notation



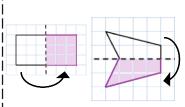
How far left or right to move Negative value (left) Positive value (right)

> How far up or down to move Negative value (down) Positive value (up)



Every vertex has been translated by the same amount

#### Compare rotations and reflections

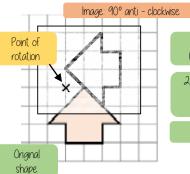


Reflections are a mirror image of the original shape.

Information needed to perform a reflection

- Line of reflection (Mirror line)

#### Rotate from a point (outside a shape)



I Trace the original shape (mark the point of rotation)

П

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2. Keep the point in the same place and turn the tracing

3. Draw the new shape

Rotations are the movement of a shape in a circular motion

#### Information needed to perform a rotation:

- Point of rotation
- Direction of rotation
- Degrees of rotation

### YEAR 9 - REASONING WITH GEOMETRY

# Enlargement & Similarity

### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Recognise enlargement and similarity
- Enlarge a shape by a positive SF
- Enlarge a shape from a point
- Enlarge a shape by a fractional SF
- Work out missing sides and angles in a pair of similar shapes.

### ! Keywords

Similar Shapes: shapes of different sizes that have corresponding sides in equal proportion and identical corresponding angles.

Scale Factor: the multiple describing how much a shape has been enlarged

**Enlarge**: to change the size of a shape (enlargement is not always making a shape bigger)

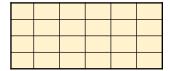
Corresponding: objects (or sides) that appear in the same place in two similar situations.

**Image**: the picture or visual representation of the shape

#### Recognise enlargement & similarity

Shapes are similar if all pairs of corresponding sides are in the same ratio

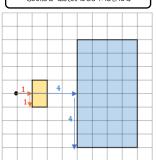
These shapes are similar because all sides are increased by the same ratio



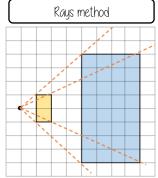
Enlargements are similar shapes with a ratio other than I

#### Enlarge a shape from a point

Scaled distances method



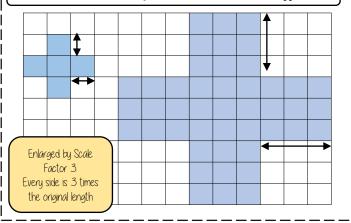
Scale the distance between the point of enlargement and each corresponding



Multiply the distance from the centre of corresponding vertices by the scale factor along the ray

#### Enlarge by a positive scale factor

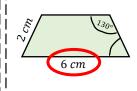
With a scale factor larger than 1 it makes the shape bigger

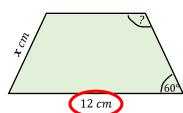


#### ============= Calculations in similar shapes

Don't forget that properties of shapes don't change with enlargements or in

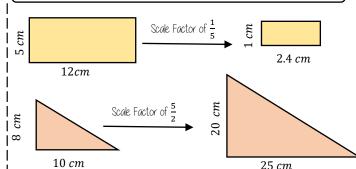
The two trapezium are similar find the missing side and angle





#### Positive fractional scale factor

With a scale factor between 0 and 1 it makes the shape smaller



Corresponding sides identify the scale factor

$$\frac{12}{6} = 2$$

Scale Factor = 2

Calculate the missing side

Length (corresponding side) x scale factor

 $2cm \times 2$ 

x = 4cm

Enlargement does not change angle size

Calculate the missing angle

Corresponding angles remain the same 130°

# YEAR 9 - CONSTRUCTING IN 2D/3D

# 3D Shapes

#### What do I need to be able to do?

By the end of this unit you should be able to:

- Name 2D & 3D shapes
- Recognise Prisms
- Sketch and recognise nets
- Draw plans and elevations
- Find areas of 2D shapes
- Find Surface area for cubes, cuboids, triangular prisms and culinders
- Find the volume of 3D shapes

#### Keywords

2D: two dimensions to the shape e.g. length and width

3D: three dimensions to the shape e.a. length, width and height

Vertex: a point where two or more line segments meet

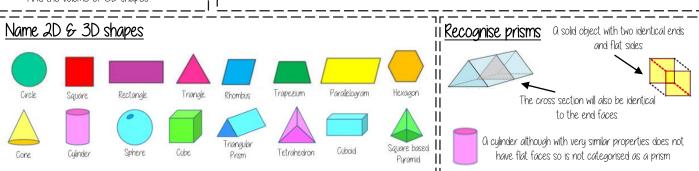
Edge a line on the boundary joining two vertex

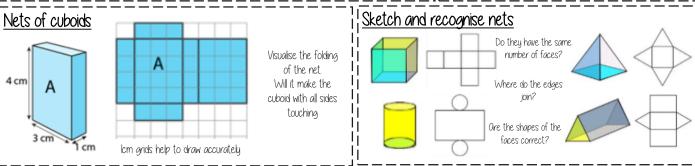
Face: a flat surface on a solid object

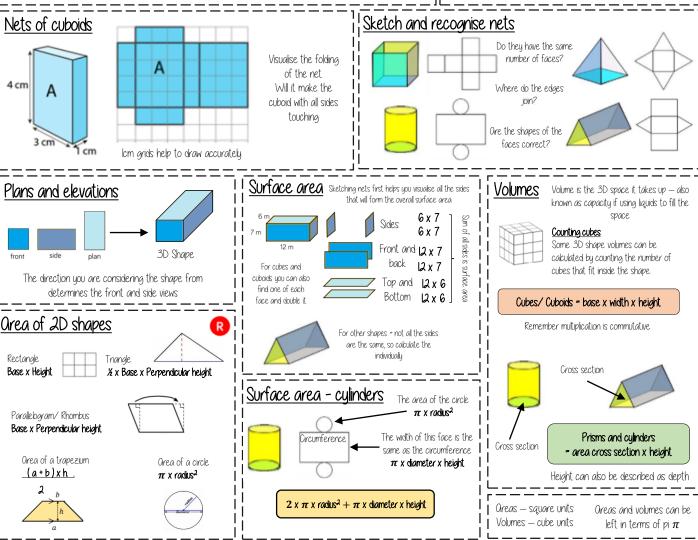
Cross-section: a view inside a solid shape made by cutting through it

Plan: a drawing of something when drawn from above (sometimes birds eye view)

Perspective: a way to give illustration of a 3D shape when drawn on a flat surface.







## YEAR 9 - CONSTRUCTING IN 2D/3D.

# Constructions & congruency

### What do I need to be able to do?

By the end of this unit you should be able to:

- Draw and measure angles
- Construct scale drawings
- Find locus of distance from points, lines, two
- Construct perpendiculars from points, lines, anales
- Identify congruence
- Identify congruent triangles

### <u>Keywords</u>

Protractor: piece of equipment used to measure and draw angles

Locus: set of points with a common property

Eauidistant: the same distance

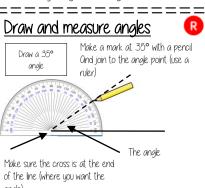
**Discorectanale**: (a stadium) — a rectangle with semi circles at either end

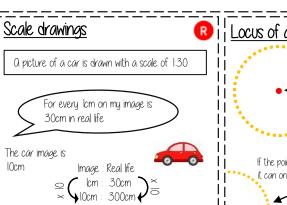
Perpendicular: lines that meet at 90°

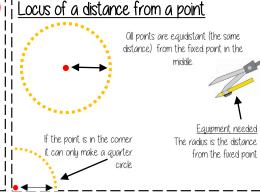
arc: part of a curve

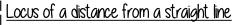
**Bisector**: a line that divides something into two equal parts

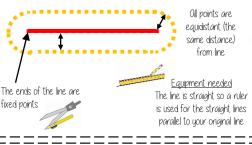
Congruent: the same shape and size











Olso an angle bisector

This cuts the angle in half

From the anale vertex draw two arcs that cut the lines forming the angle

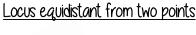
Keep the compass the same size and use

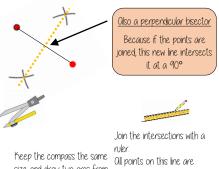
the new arcs as centres to draw

Join the vertex to the intersection

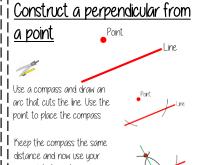
intersecting arcs in the middle

ocus of a distance from two lines





equidistant from both points



new points to make new interconnecting arcs

Connecting the arcs makes the bisector

#### Conaruent fiaures

size and draw two arcs from



Congruent figures are identical in size and shape — they can be reflections or rotations of each

#### Congruent triangles



Oll three sides on the triangle are the same size

#### Ongle-side-angle

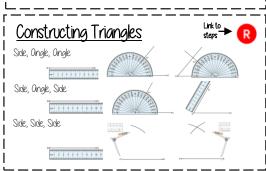
Two angles and the side connecting them are equal in two triangles

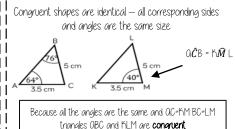
#### Side-angle-side

Two sides and the angle in-between them are equal in two triangles (it will also mean the third side is the same size on both shapes)

#### Right angle-hypotenuse-side

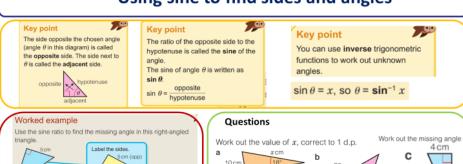
II The triangles both have a right angle, the hypotenuse and one side are the same

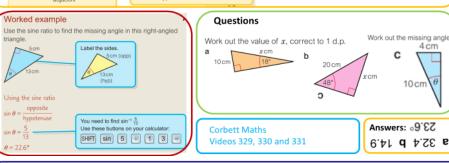


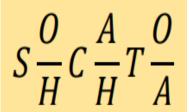


# YEAR 9 — Trigonometry

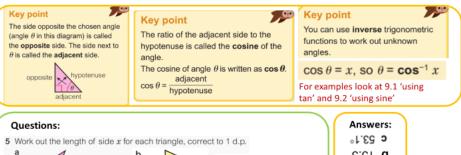


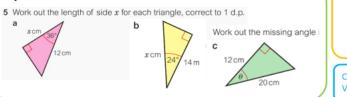












The ratio of the opposite side to the

adjacent side is called the tangent

Key point

of the angle.

The side opposite the chosen angle

the opposite side. The side next to

(angle  $\theta$  in this diagram) is called

### 5.31 d 7.9 B

Corbett Maths Videos 329, 330 and 331

Hint for Qb:

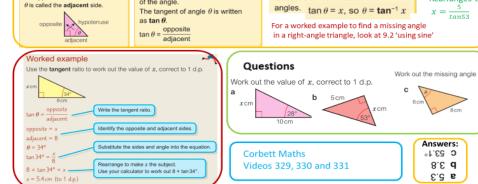
Rearranges to

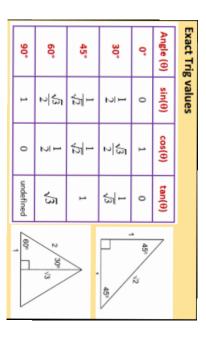
 $Tan53 = \frac{5}{}$ 

#### Using tangent to find sides and angles

You can use inverse trigonometric

functions to work out unknown





### YEAR 9 - REPRESENTATIONS.

# Probability

#### What do I need to be able to do?

By the end of this unit you should be able to:

- Find single event probability
- Find relative frequency
- Find expected outcomes
- Find independent events
- Use diagrams to work out probabilities

### Keywords

Probability: the chance that something will happen

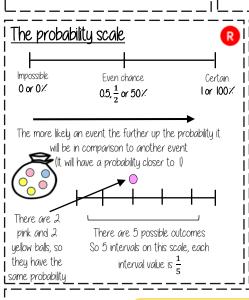
Relative Frequency: how often something happens divided by the outcomes

**Independent**: an event that is not effected by any other events.

Chance: the likelihood of a particular outcome.

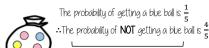
**Event**: the outcome of a probability — a set of possible outcomes.

Biased: a built in error that makes all values wrong by a certain amount.



#### 🔃 I Single event probabilitu

Probability is always a value between 0 and 1

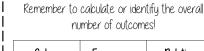


The sum of the probabilities is 1

The table shows the probability of selecting a type of chocolate

Dark	Milk	White
0.15	0.35	

P(white chocolate) = 1 - 0.15 - 0.35



Relative Frequency

Colour	Frequency	Relative Frequency
Green	6	0.3
Yellow	12	0.6
Blue	2	0.1

Frequency of event Total number of outcomes

Relative frequency can be used to find expected

20

e.g. Use the relative probability to find the expected outcome for green if there are 100 selections.

Relative frequency x Number of times  $0.3 \times 100 = 30$ 

#### Expected outcomes

Expected outcomes are estimations. It is a long term average rather than a prediction.

Dark	Milk	White	
0.15	0.35	0.5	

The sum of the probabilities is 1

On experiment is carried out 400 Show that dark chocolate is expected

to be selected 60 times

 $0.15 \times 400 = 60$ 

#### Independent events



The rolling of one dice has no impact on the rolling of the other. The individual probabilities should be calculated separately.

#### Probability of event 1 × Probability of event 2





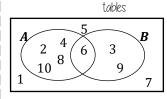
$$P(R) = \frac{1}{4}$$

Find the probability of getting a 5 and

$$P(5 \text{ and } R) = \frac{1}{6} \times \frac{1}{4} = \frac{1}{24}$$

#### Using diagrams Recap Venn diagrams, Sample space diagrams and Two-way

Ш



	Car	Bus	Walk	Total
Boys	15	24	14	53
Girls	6	20	21	47
Total	21	44	35	100

The possible outcomes from rolling a dice

E 3	ই					1		
. outcom	ව 2 2		1	2	3	4	5	6
possibile m tossir	Н	ľΉ	2,H	3,H	4,H	5,H	6,H	
ne possipie oucom from tossing a coir	T	ļΤ	2,T	3,T	4,T	5,T	6,T	