Algebra - Foundation

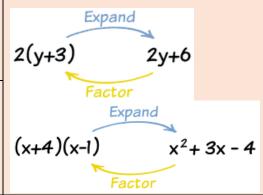
Notation

 $ab = a \times b$ $a^2 = a \times a$ $(2a)^3 = 2a \times 2a \times 2a$ $(a + b)^2 = (a + b)(a + b)$

Definitions

Expression – no equal signs e.g. 2x + 3, 2y, $(3x - 2)^2$ Equations – equal signs, can be solved, e.g. y + 4 = 10Identities – identical/equivalent to e.g. $2(y + 4) \equiv 2y + 8$ Formulae – equal signs, more than one unknown e.g. $A = \frac{1}{2}bh$

Factorising and expanding



Straight line graphs

y = mx + c m = gradientc = y - intercept



negative gradient

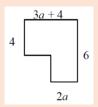
$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{change \ in \ y}{change \ in \ x}$$

Parallel lines – have equal gradients

Simplifying expressions by collecting like terms

Always circle the sign IN FRONT of the term to avoid errors.

$$3x - 7b - x + 9b \equiv 2x + 2b$$



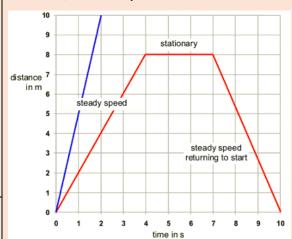
Typical Exam Q: Create an expression for the perimeter of the shape by adding and collecting like terms.

If the perimeter is given as 20cm, for example, you can create an equation:

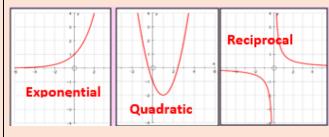
$$4 + 3a + 4 + 6 + 2a = 20$$

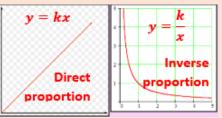
 $5a + 14 = 20$

Distance / Time Graphs



Graphs that need to be recognised



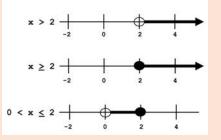


Simplifying expressions multiplication and division

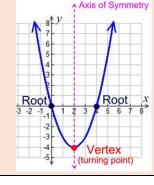
$$2ma^2 \times 7ma = 14m^2a^3$$

$$\frac{18b^6}{3ab^2} = \frac{6b^4}{a}$$

Inequalities



Open circle: </>Closed circle: \le/\ge Turning point and roots of a quadratic equation



Finding the nth term of a linear sequence

5, 7, 9, 11, 13,

- 1. Find the common difference: 2
- 2. This is the coefficient of n: 2n
- 3. Find the difference between the coefficient of n and the first term 5-2=3
- 4. Add this to the amount of n

Geometry and Measures - Foundation

Trigonometry

$$S\frac{O}{H}C\frac{A}{H}T\frac{O}{A}$$

Example - finding a side:

$$\sin 37 = \frac{x}{5}$$

 $x = 5 \times \sin 37^{\circ}$



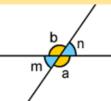
Example – finding a side:

$$\tan y = \frac{3.2}{7.1}$$

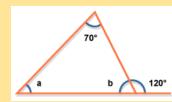
$$y = tan^{-1} \left(\frac{3.2}{7.1}\right).$$



Angle Facts



Vertically opposite angles are equal: a=b and m=n



Angles in a triangle sum to 180°.

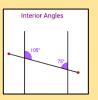
Angles on a straight line sum to 180°.

E.G: $b=60^{\circ}$ so $a=50^{\circ}$

Angles in parallel lines







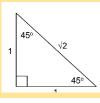
Corresponding angles are equal

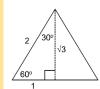
Alternate angles are equal

Co-interior angles add to 180.

Exact Trig values

Angle (θ)	sin(θ)	cos(θ)	tan(θ)
0°	0	1	0
30°	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{3}}$
45°	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$	1
60°	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\sqrt{3}$
90°	1	0	undefined





Simple vector notation

 $\binom{a}{b}$

a: movement along the x-axis (left or right)b: movement along the y-axis (up or down)

-a: movement left

-b: movement down

Operations with vectors

$$\binom{2}{6} + \binom{7}{-3} = \binom{9}{3}$$

If $b = \binom{4}{-2}$, then $3b = \binom{12}{-6}$

Volume & surface area

Volume = area of cross section x length

Surface area = area of all the faces of a 3D shape

Learn the cylinder

$$V = \pi r^2 h$$
$$SA = 2\pi r^2 + \pi dl$$

Types of triangles

Right angled Isosceles Equilateral Scalene

Types of quadrilaterals

Square Rectangle Parallelogram Rhombus Trapezium Kite

Area of key shapes

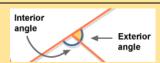
Triangle : $A = \frac{b \times h}{2}$ (h = perpendicular height)

Parallelogram: A = b x h (h = perpendicular height)

Trapezium: $A = \left(\frac{a+b}{2}\right) \times h$ (add together the parallel sides, divide the total by 2, and then multiply by the perpendicular height between the parallel sides)

Angles in regular polygons

n = number of sides

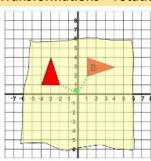


Interior angle + exterior angle = 180^o

Exterior angle =
$$\frac{360}{n}$$

$$n = \frac{360}{Exterior \ angle}$$

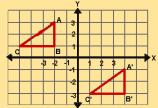
Transformations – rotation



Always use tracing paper. Describe:

- 1. It's a rotation
- 2. Size of rotation in degrees
- 3. Orientations: clockwise or anticlockwise
- 4. Centre of rotation given as a coordinate (x,y)

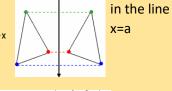
Transformations – translations and reflections



Translate triangle

ABC to A'B'C' with

the vector $\binom{6}{4}$

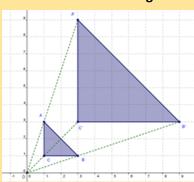


Line of Reflection

Reflection

Reflection in the line y=a

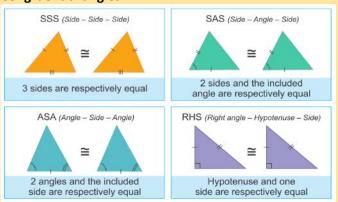
Transformations - enlargement



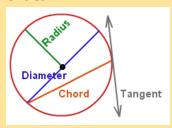
Describe:

- 1. It's an enlargement
- 2. The scale factor (if the image is smaller than the object the scale factor is fractional e.g. ½)
- 3. The centre of enlargement given as a coordinate

Congruent triangles



Circles





Sector $Area = \frac{\theta}{360}\pi r^2$

 $Circumference = \pi d$

Arc length =
$$\frac{\theta}{360}\pi d$$

Pythagoras' Theorem

$$a^2 + b^2 = c^2$$

Only applies to right angled triangles.

Can be used to find the height of an isosceles triangle

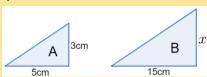


Can be used to find the length distance between two coordinates

Similar shapes

Same shape, different sides

The ratio of the lengths of corresponding sides are equal



Length scale factor = $15 \div 5 = 3$

x = 3 cm x 3

3D notation

Cube:

Faces: 6



Edges: 12



Vertices: 8

Square based pyramid:



Bearings

Measure from the North Measured in a clockwise direction Written using 3 digits

Bearing of B from A (start at A)



Bearing of A from B (start at B)



Number Ratio and Proportion - Foundation

Estimate

Round each value to one significant figure

Standard form

 $a \times 10^n$, where $1 \le a < 10$

Reciprocal

Reciprocal of 7 is $\frac{1}{7}$, reciprocal of $\frac{2}{3}$ is $\frac{3}{2}$ etc

Sequences

Fibonacci sequence: 1, 1, 2, 3, 5, 8, 13, 21

Geometric Sequence: each term is multiplied but he same constant to get the next number.

E.g. 3, 12, 48, 191, (x by 4 each time)

Simplifying Ratio

Divide both sides by the highest common factor



Simplifying Ratio 1:n

Divide both sides by the highest factor of the left hand side

2m: 180cm 200cm: 180cm 2:1.8 1: 0.9

Squares and Cubes

Square numbers: 1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225 etc

Cube numbers: 1, 8, 27, 64, 125, 216, 343, 512, etc

Sharing in a given Ratio

A Add the ratio parts

D Divide the amount by the total parts

A and

M Multiply the ratio by the value of one part

e.g. share £420 in the ratio 2:5

Fractions

Add and Subtract – ensure the fractions have the same denominator before adding numerators

$$\frac{4}{5} - \frac{1}{3} = \frac{12}{15} - \frac{5}{15} = \frac{7}{15}$$

Multiply – multiply numerators and denominators

$$\frac{4}{5} \times \frac{1}{3} = \frac{4}{15}$$

Divide – take reciprocal of the second fraction and then multiply the new numerators and denominators

$$\frac{4}{5} \div \frac{1}{3} = \frac{4}{5} \times \frac{3}{1} = \frac{12}{5} = 2\frac{2}{5}$$

Percentages

Finding percentages of an amount

1% ÷100 5% ÷20 20% ÷5 25% ÷4 50% ÷2

Multipliers:

To find the multiplier for a percentage, divide by 100

Use multipliers on a calculator paper e.g. 35% of $370 = 0.35 \times 370$

Increasing and decreasing a given amount

Calculator:

 $Orginal\ Amount\ x\ mutiplier = new\ amount$

Non-calculator: find the increase or decrease and add to the original amount

Finding percentage increase or decrease (profit/loss)

$$\frac{value\ of\ increase\ decrease}{Original} \times 100$$

Writing an amount as a percentage of the original

$$\frac{Amount}{Original} \times 100$$

Reverse Percentage – finding the original amount

$$Orginal\ Amount = \frac{New\ Amount}{multiplier}$$

Growth & Decay / Compound interest	Dividing by decimals:	Conversions
	Write the calculation as a fraction	10 millimetres = 1 centimetre 15 minutes = 0.25
original amount $ imes$ multiplier time	2. Form an equivalent fraction to makes integers	hours
	(multiply by powers of 10)	100 centimetres = 1 metre 30 minutes = 0.5
Where the multiplier is the percentage, increase or	3. Use short division (bus stop) to calculate	hours
decrease from 100%, converted to a decimal.		1000 metres = 1 kilometre 45 minutes = 0.75
e.g.	e.g. $460 \div 0.4 = \frac{460}{0.4} = \frac{4600}{4} = 1150$	hours
30% decrease is 70% = 0.7	0.4 4	1000cm ³ = 1 litre
30% increase is 130% = 1.3		1000ml = 1 litre
Compound Units (rearrange as necessary)	Error Intervals	Negative numbers
	least possible value $\leq x <$ greatest possible value	Adding and subtracting: (vertical number lines help)
Distance		-3 - 5 = -8
$Speed = \frac{Distance}{Time}$	e.g. A fence is 30 m long to the nearest 10 m.	-3 + 5 = 2
Time	$25 \text{ m} \le l < 35 \text{ m}$	-3 5 = -3 + 5 = 2
		-3 - + 5 = -3 - 5 = -8
$Area = \frac{Force}{Pressure}$	Truncation	-3 + - 5 = -3 - 5 = -8
Pressure	Truncation is a method of approximating a decimal	
	number by dropping all decimal places past a certain	Multiplying and dividing:
	point without rounding.	Different signs – answer will be negative
$Density = \frac{Mass}{Volume}$		+ x - = -, - x + = -
Volume	e.g. Truncate 3.14159265 to 4 decimal places.	Same signs – answer will be positive
	= 3.1415	- X - = +
Ordering fractions	Order of operations	Rounding to significant figures
Calc: use division to write each fraction as a decimal	B racket	Start from the first non-zero number and round as
Non-calc: write fractions with common denominators	Indices	normal, but ensure the place value is correct
	D ivision and M ultiplication	e.g. 345,635 to 2SF = 350,000
	Addition and Subtraction	0.0060821 to 3SF = 0.0608
Index Laws	Prime Factorisation HCF and	LCM of 90 and 120 (Factor Tree & Venn Diagram)
$a^n \times a^m - a^{n+m}$	HCF is the	nroduct of common factors

$$a^{n} \times a^{m} = a^{n+m}$$

$$a^{n} \div a^{m} = a^{n-m}$$

$$(a^{n})^{m} = a^{nm}$$

$$a^{0} = 1$$

$$a^{-n} = \frac{1}{a^{n}}$$

$$a^{\frac{n}{m}} = \sqrt[m]{a^{n}}$$

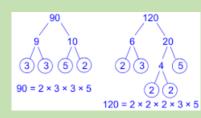
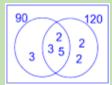


Diagram)

HCF is the product of common factors

LCM is the product of common factors and remaining factors.



HCF: 2x3x5 LCM: 2³x3²x5

Probability and Statistics - Foundation

Averages

Mode: most common piece of data

Mean: Sum of the data ÷ total frequency

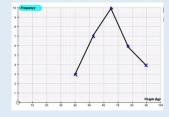
Median: order the data and find the middle value

Range: Highest value – lowest value

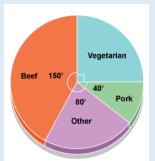
Frequency Polygons

- 1. Plot frequency at the mid-point
- 2. Join with straight lines

Weight w (kg)	Frequency
30 ≤ w < 50	3
50 ≤ w < 55	7
55 ≤ w < 75	10
75 ≤ w < 80	6
80 ≤ w < 100	4



Reading and Drawing Pie Charts



Find the fraction of the total

1000 people were surveyed

Beef:
$$\frac{150}{360} \times 1000$$

Vegetarian: $\frac{90}{360} \times 1000$

Hair colour	People
Blonde	8
Brown	12
Red	3
Grey	2
Black	6

Find the fraction of the full circle.

Size of Blonde sector: $\frac{8}{31} \times 360^{\circ}$

Averages from a frequency table

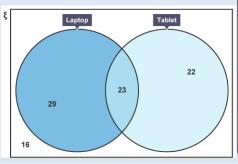
Mean: $\frac{\sum fw}{\sum f}$; where, w is the midpoint of the group.

Median group: find which group the $\frac{n+1}{2}th$, value lies. Where, n is the total frequency.

E.G. in this table 51.5th value which lies in group $8 < w \le 12$ (using the cumulative frequency

Weight of box (w kg)	Frequency
0 < w ≤ 4	11
4 < w ≤ 8	16
8 < w ≤ 12	29
12 < w ≤ 16	26
16 < w ≤ 20	20

Venn Diagrams



Information given:
90 pupils were
surveyed
52 said they owned
a laptop.
45 said they owned
a tablet.
23 said they owned
both.

Expected outcomes

Expected outcome = probability x number of trials

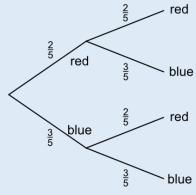
E.g. A biased spinner is spun 800 times. The probabilities is lands on each colour is below. The probability of it landing on red is the same as the probability of it landing on green. How many times would you expect yellow to come up.

Result	Red	Green	Brown	Yellow
Probability		0.48	0.2	

$$P(Y) = (1 - 0.48 - 0.2) \div 2 = 0.32 \div 2 = 0.16$$

Expected yellow = $0.16 \times 800 = 128$

Tree diagrams



Multiply along the branches to find each probability.

- 1. Probability that a red counter is picked both times $P(RR) = \frac{2}{5} \times \frac{2}{5} = \frac{4}{25}$
- 2. Probability that the counters are different colours = P(RB) + P(BR) = $\frac{2}{5}$ x $\frac{3}{5}$ + $\frac{3}{5}$ x $\frac{2}{5}$ = $\frac{12}{25}$

Probability Definitions

Total probability: adds to 1

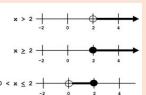
Relative frequency: $frequency \div total \ trials$

Independent events: one event doesn't impact the other

Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Linear Inequalities



Open circle: </>>

Closed circle: \leq / \geq

Algebriac proof – toolkit

Even numbers: 2n, 2n+2, 2n+4,... Odd numbers: 2n+1, 2n+3, 2n+5,...

Sum: add

Product: multiply Difference: subtract

Show it's a multiple: factorise

Show it's even: show it's a multiple of 2 Show it's odd: show it's a multiple of 2, plus 1

Straight line graphs

$$y = mx + c$$

 $m = gradient$
 $c = y - intercept$

positive gradient

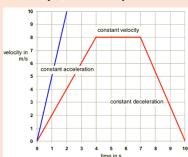
negative gradient

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{change \ in \ y}{change \ in \ x}$$

Parallel lines – have equal gradients

Perpendicular lines – If L₁ and L₂ are perpendicular then $m_2 = -\frac{1}{m_1}$

Velocity / Time Graphs



Iteration – showing a root lies between 2 points:

If there is a change in sign for y for two particular values of

x then we can say there is a root between these values of x

Gradient = acceleration

Area = distance travelled

Completing the square

Quadratic expression factorised by completing the square:

$$(x+a)^2+b$$

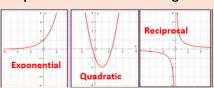
Turning point of graph occurs at (-a, b)

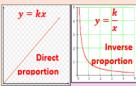
Solve quadratic inequalities

e.g solve $x^2 + 5x - 24 \ge 0$

- 1. Factorise: $(x + 8)(x 3) \ge 0$
- 2. Solve: x = -8, x = 3
- 3. Sketch the graph
- 4. Values that satisfy the inequality $x \le -8$, $x \ge 3$

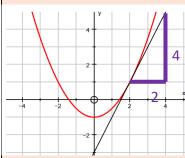
Graphs that need to be recognised:





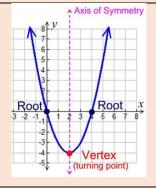
and we can say that the equation f(x) = 0 will have a solution between these two values of x.

Gradients of curves



Gradient of a curve at a point = gradient of the tangent at the point

Turning point and roots of a quadratic equation



Equation of a circle centre (0, 0) $x^2 + y^2 = r^2$

Functions

f(4): Substitute 4 into the function

f(g(x)): Substitute g(x) into f(x) i.e. replace all values of x in f(x) with the entire function g(x)

e.g.
$$f(x) = 2x + 3$$
, $g(x) = x - 3$, $fg(x) = 2(x-3) + 3$

Geometry and measure - Higher

Trigonometry

$$S\frac{O}{H}C\frac{A}{H}T\frac{O}{A}$$

Example – finding a side:

$$\sin 37 = \frac{x}{5}$$

 $x = 5 \times \sin 37^{\circ}$



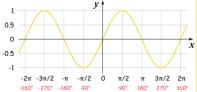
Example – finding a side:

$$\tan y = \frac{3.2}{7.1}$$

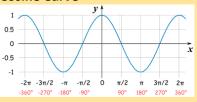
$$y = tan^{-1} \left(\frac{3.2}{7.1} \right).$$



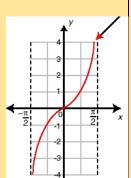
Sine Curve



Cosine Curve



Tangent Curve



Angles in parallel lines







Corresponding angles are equal

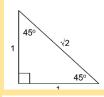
Alternate angles are equal

Volume & surface area

Co-interior angles add to 180.

Exact Trig values

Angle (θ)	sin(θ)	cos(θ)	tan(θ)
0°	0	1	0
30°	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{3}}$
45°	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$	1
60°	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\sqrt{3}$
90°	1	0	undefined





Simple vector notation

a: movement along the x-axis (left or right)

b: movement along the y-axis (up or down)

-a: movement left

 $\binom{2}{6} + \binom{7}{-3} = \binom{9}{3}$

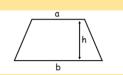
Operations with vectors

-b: movement down

Area of a trapezium

Learn the cylinder

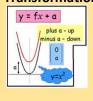
$$A = \frac{1}{2}(a+b)h$$

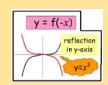


 $V = \pi r^2 h$

 $SA = 2\pi r^2 + \pi dl$

Transformation of a graph





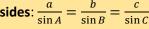


Sine rule

angles:
$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

sides: $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

If $b = \binom{4}{-2}$, then $3b = \binom{12}{-6}$



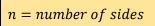
Cosine rule

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Area of a triangle

$$\frac{1}{2}ab\sin C$$

Angles in regular polygons



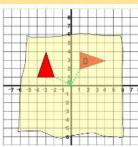


Interior angle + exterior angle = 180°

Exterior angle =
$$\frac{360}{n}$$

$$n = \frac{360}{Exterior \ angle}$$

Transformations - rotation - describing:



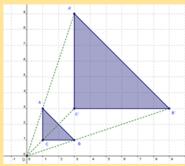
Always use tracing paper. Describe:

- 1. It's a rotation
- 2. Size of rotation in degrees
- 3. Orientations: clockwise or anticlockwise
- 4. Centre of rotation given as a coordinate (x,y)

Transformation - translation

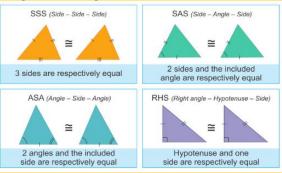
Transformations - enlargement - describing:

- 1. It's an enlargement
- 2. The scale factor (if the image is smaller than the object the scale factor is fractional e.g. ½)
- 3. The centre of enlargement given as a coordinate

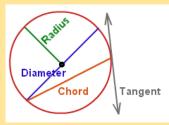


Vector $\binom{6}{-4}$ 6 right, 4 down

Congruent triangles



Circles



$$Area = \pi r^2$$

 $Circumference = \pi d$

Sector
$$Area = \frac{\theta}{360}\pi r^2$$

Arc length = $\frac{\theta}{360}\pi d$

Similar shapes

Same shape, different sides The ratio of the lengths of corresponding sides are equal

Length scale factor = x

Area scale factor = x^2

Volume scale factor = x^3

Pythagoras' Theorem

$$a^2 + b^2 = c^2$$

Only applies to right angled triangles.

Can be used to find the height of an isosceles triangle



Can be used to find the length distance perween two coordinates

Circle Theorems



Angle at the centre is twice the angle at the circumference



Angles in a semicircle are 90°.



Angles in the same segment are egual.



Opposite angles of a cyclic quadrilateral add up to 180.



Alternate segment theorem.



Tangents from an external point are equal in length.

The tangent to a circle is perpendicular (90°) to the radius

Number Ratio and Proportion - Higher

Number Ratio and Proportion - Higher
Estimate Round each value to one significant figure

Standard form $a \times 10^n$, where $1 \le a < 10$

Reciprocal

Reciprocal of 7 is
$$\frac{1}{7}$$
, reciprocal of $\frac{2}{3}$ is $\frac{3}{2}$ etc

Sequences

Fibonacci sequence: 1, 1, 2, 3, 5, 8, 13, 21

Geometric Sequence: each term is multiplied but he same constant to get the next number.

E.g. 3, 12, 48, 191, (x by 4 each time)

Recurring Decimals

Form two equations where the digits following the decimal point are the same, and therefore can be cancelled

Upper and lower bounds

Look at the value above and below for the same place value. LB and UB will be half way between these points

e.g. 17 rounded to the nearest integer



e.g. 24.6 roudned to one decimal place.

Simplifying Surds

Find a factor that is a square number

$$\sqrt{96} = \sqrt{16 \times 6} = 4\sqrt{6}$$

Manipulating surds

$$\sqrt{ab} = \sqrt{a} \times \sqrt{b}$$

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$

Rationalising Surds

Rationalise by removing any surds from the denominator

E.G with surd.

$$\frac{2\sqrt{3}}{\sqrt{5}} = \frac{2\sqrt{3} \times \sqrt{5}}{\sqrt{5} \times \sqrt{5}} = \frac{2\sqrt{3} \times 5}{\sqrt{5} \times 5} = \frac{2\sqrt{15}}{\sqrt{25}} = \frac{2\sqrt{15}}{5}$$

E.G with surd expressions multiply by top and bottom by the denominator with the opposite sign.

$$\frac{5}{3+\sqrt{2}} = \frac{5 \times (3-\sqrt{2})}{(3+\sqrt{2}) \times (3-\sqrt{2})} = \frac{5(3-\sqrt{2})}{9-\sqrt{4}}$$
$$= \frac{5(3-\sqrt{2})}{7}$$

Fractions

Add and Subtract – ensure the fractions have the same denominator before adding numerators

$$\frac{4}{5} - \frac{1}{3} = \frac{12}{15} - \frac{5}{15} = \frac{7}{15}$$

Multiply – multiply numerators and denominators

$$\frac{4}{5} \times \frac{1}{3} = \frac{4}{15}$$

Divide – take reciprocal of the second fraction and then multiply the new numerators and denominators

$$\frac{4}{5} \div \frac{1}{3} = \frac{4}{5} \times \frac{3}{1} = \frac{12}{5} = 2\frac{2}{5}$$

Percentages

Finding percentages of an amount

Multipliers:

To find the multiplier for a percentage, divide by 100

Use multipliers on a calculator paper e.g. 35% of $370 = 0.35 \times 370$

Increasing and decreasing a given amount

Calculator:

 $Orginal\ Amount\ x\ mutiplier = new\ amount$

Non-calculator: find the increase or decrease and add to the original amount

Finding percentage increase or decrease (profit/loss)

$$\frac{value\ of\ increase/decrease}{Original} \times 100$$

Writing an amount as a percentage of the original

$$\frac{Amount}{Original} \times 100$$

Reverse Percentage – finding the original amount

$$Orginal\ Amount = \frac{New\ Amount}{multiplier}$$

Growth & Decay / Compound interest	Dividing by decimals:	Conversions
	Write the calculation as a fraction	10 millimetres = 1 centimetre 15 minutes = 0.25
original amount $ imes$ multiplier $^{ ext{time}}$	Form an equivalent fraction to makes integers	hours
	(multiply by powers of 10)	100 centimetres = 1 metre 30 minutes = 0.5
Where the multiplier is the percentage, increase or	3. Use short division (bus stop) to calculate	hours
decrease from 100%, converted to a decimal.		1000 metres = 1 kilometre 45 minutes = 0.75
e.g.	e.g. $460 \div 0.4 = \frac{460}{0.4} = \frac{4600}{4} = 1150$	hours
30% decrease is 70% = 0.7	0.4 4	1000cm ³ = 1 litre 1000g = 1 kilogram
30% increase is 130% = 1.3		1000ml = 1 litre
Compound Units (rearrange as necessary)	Error Intervals	Negative numbers
	least possible value $\leq x <$ greatest possible value	Adding and subtracting: (vertical number lines help)
Distance		-3 – 5 = -8
$Speed = rac{Distance}{Time}$	e.g. A fence is 30 m long to the nearest 10 m.	-3 + 5 = 2
1 61166	$25 \text{ m} \le l < 35 \text{ m}$	-3 5 = -3 + 5 = 2
		-3 - + 5 = -3 - 5 = -8
$Area = \frac{Force}{}$	Truncation	-3 + - 5 = -3 – 5 = -8
$Area = \frac{rorec}{Pressure}$	Truncation is a method of approximating a decimal number	
	by dropping all decimal places past a certain point without	Multiplying and dividing:
.,	rounding.	Different signs – answer will be negative
$Density = \frac{Mass}{Volume}$	e.g. Truncate 3.14159265 to 4 decimal places.	+ x - = -, - x + = -
Volume	= 3.1415	Same signs – answer will be positive
		- x - = +
Product rule	Order of operations	Rounding to significant figures
If there are m ways to do one thing and n ways to do	Bracket	Start from the first non-zero number and round as
another, then there are $m \times n$ ways to do both	Indices	normal, but ensure the place value is correct
	Division and Multiplication	e.g. 345,635 to 2SF = 350,000
	Addition and Subtraction	0.0060821 to 3SF = 0.0608
Index Laws		CM of 90 and 120 (Factor Tree & Venn Diagram)
$a^n \times a^m = a^{n+m}$	HCF is the p	roduct of common factors

$$a^{n} \times a^{m} = a^{n+m}$$

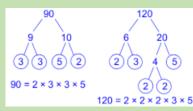
$$a^{n} \div a^{m} = a^{n-m}$$

$$(a^{n})^{m} = a^{nm}$$

$$a^{0} = 1$$

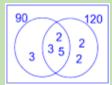
$$a^{-n} = \frac{1}{a^{n}}$$

$$a^{\frac{n}{m}} = \sqrt[m]{a^{n}}$$



HCF is the product of common factors

LCM is the product of common factors and remaining factors.

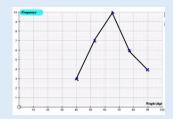


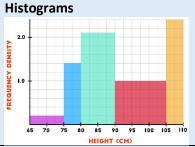
HCF: 2x3x5 LCM: 2³x3²x5

Frequency Polygons

- 1. Plot frequency at the mid-point
- 2. Join with straight lines

Weight w (kg)	Frequency
30 ≤ w < 50	3
50 ≤ w < 55	7
55 ≤ w < 75	10
75 ≤ w < 80	6
80 ≤ w < 100	4

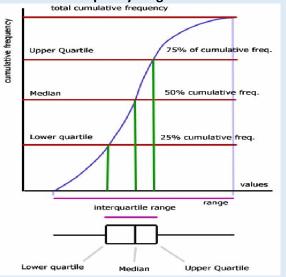




FD = Frequency density

$$FD = \frac{Frequency}{Class Width}$$

Cumulative Frequency Diagrams and Box Plots



Averages from a frequency table

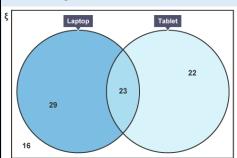
Mean: $\frac{\sum fw}{\sum f}$; where, w is the midpoint of the group.

Median group: find which group the $\frac{n+1}{2}th$, value lies. Where, n is the total frequency.

E.G. in this table 51.5th value which lies in group $8 < w \le 12$ (using the cumulative frequency

Weight of box (w kg)	Frequency
0 < w ≤ 4	11
4 < w ≤ 8	16
8 < w ≤ 12	29
12 < w ≤ 16	26
16 < w ≤ 20	20

Venn Diagrams



Information given: 90 pupils were surveyed 52 said they owned a laptop.

45 said they owned a tablet.

23 said they owned both.

Expected outcomes

Relative frequency: $frequency \div total \ trials$

Expected outcome = probability x number of trials

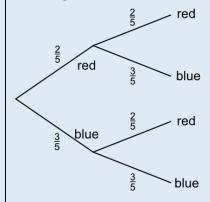
E.g. A biased spinner is spun 800 times. The probabilities is lands on each colour is below. The probability of it landing on red is the same as the probability of it landing on green. How many times would you expect yellow to come up.

Result	Red	Green	Brown	Yellow
Probability		0.48	0.2	

$$P(Y) = (1 - 0.48 - 0.2) \div 2 = 0.32 \div 2 = 0.16$$

Expected yellow = $0.16 \times 800 = 128$

Tree diagrams



Multiply along the branches to find each probability.

- 1. Probability that a red counter is picked both times $P(RR) = \frac{2}{5} \times \frac{2}{5} = \frac{4}{25}$
- 2. Probability that the counters are different colours = P(RB) + P(BR) = $\frac{2}{5}$ x $\frac{3}{5}$ + $\frac{3}{5}$ x $\frac{2}{5}$ = $\frac{12}{25}$

Notation

A – all elements in A

A' – all elements **not in A**

B - all elements in B

B' - all elements not in B

A U B – all the elements in A or B or both

A \(\text{B} - \text{all the elements in both A and B} \)